Grasping and Manipulation

- Prehensile tactile proprioceptive
- Traction response
- Reflexive squeeze
- Optical and labyrinthine-righting
- Lateral propping
- Raking
- Positive support
- Mature stepping
- 3-jaw chuck
- Pincer isolation
- Forefinger isolation
- Inferior pincer
- Radial digital
- Scissors
- Radial palmar
- Crude palmar
- Palmar grasp reflex
- ATNR
- Galant ATNR
- Landau STNR
- STNR
- Amphibian segmental rolling
- Body-on-head reflex
- Postural stability vestibular proprioceptive visual
- Neonate
- Instinctive grasp reaction
- Release responses
- Avoiding response
- Prehensile palmar

MONTHS
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

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Grasping and Manipulation

Grasp

Power
- clamping not required
- emphasis on security, stability

Non-Prehensile
- Hook, Platform, Push
- Large Diameter

Prehensile
- clamping required

Circular
- radial symmetry, 3 virtual fingers
- Small Diameter

Prismatic
- wrap symmetry, fingers surround part
- radial symmetry, fingers surround part
- Medium Wrap
- Adducted Thumb
- Light Tool
- Disk
- Sphere
- Tripod

Specific Grasps
- italic labels - grasp attributes
- boldface labels - grasp names

Increasing Power and Object Size

Increasing Dexterity, Decreasing Object Size
Haptics

• concerns the sense of touch—in particular, the perception and manipulation of objects using tactile and proprioceptive feedback gathered from peripheral mechanoreceptors, kinematic and dynamic state, muscle dynamics, neural conduction, and hierarchical processing

• incorporates a wide variety of central and peripheral mechanoreceptors and neural systems that measure forces, heat flux, pain, accelerations, the degree of stretch in muscle fibers and tendons.

• the result is high-fidelity perceptual information regarding force, contact and movement, sense of shape, hardness, texture, heat flux, grasp stability, and a variety of other subjective sensations associated with contact phenomena.
...the ancient Greeks observed that muscles could be permanently disabled by severing a thin white cord called a (peripheral) *nerve* that began and ended at the spinal cord.
Intercellular Communication

indirect electrical coupling
refractory period
sodium and potassium pumps

there are places (e.g. in substantia nigra) where ions are exchanged directly (cytoplasm to cytoplasm) between cell bodies.
Mechanoreceptors

stressors come in many forms:
electrical, electromagnetic, and mechanical
variable response and sensitivity, massive redundancy

*touch blend* interpretation over multi-sensory signals temperature, pressure, and vibration ... distinguish wet, slimy, greasy, syrupy, mushy, doughy, gummy, spongy or dry, hardness, texture, compliance, size, shape, and curvature.

movement is critical to the formation of haptic images leading to active tactile exploratory strategies
## Biological Sensor Performance

<table>
<thead>
<tr>
<th>Category</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>frequency response</td>
<td>0 to 400 Hz (+ very high freq)</td>
</tr>
<tr>
<td>sensitivity</td>
<td>approx. 0.2 grams/mm²</td>
</tr>
<tr>
<td>max. response</td>
<td>100 grams/mm²</td>
</tr>
<tr>
<td></td>
<td>⇒ 55dB dynamic range*</td>
</tr>
<tr>
<td>spatial resolution</td>
<td>1.8 mm (two-point discrimination tests)</td>
</tr>
<tr>
<td>signal propagation</td>
<td>motor neurons 100 m/sec</td>
</tr>
<tr>
<td></td>
<td>sensory neurons 2 to 80 m/sec</td>
</tr>
<tr>
<td></td>
<td>autonomic neurons 0.5 to 15 m/sec</td>
</tr>
</tbody>
</table>

* - dynamic range = \(20 \log_{10}\left(\frac{P_{\text{max}}}{P_{\text{min}}}\right)\)

- sound: \(\sim 100\) dB ⇒ factor of 100,000 in amplitude and 10,000,000,000 in power
- sight: \(\sim 90\) dB ⇒ factor of 1,000,000,000 in brightness.
Robot Tactile Sensors - Desiderata

- contour vs. force sensing
- spatial resolution
- sensitivity - minimum magnitude of input signal required to produce a specified output signal-to-noise
- dynamic range - the ratio of largest to smallest detectable values
- hysteresis - “history”
  affect, plasticity
- frequency response (slip detection)
- manufacturing, durability, packaging, addressing, # wires
Binary Contact Switch

on/off contact switch, can be augmented easily to improve resolution...

Raibert (1984) increasing contact force threshold for each successive switch a prototype was constructed to produce 4 bits of pressure output per cell, serialized I/O, 200 tactile cells with a 1 mm spacing driven by 5 wires: power, ground, clock, data-in, and data-out.
Load Cells

![Diagram of a load cell with strain gauges and force, tension, and compression directions]

Six-Axis Force/Torque Sensor: typically \( n \) strain gauges mounted on a multi-axial elastic element that measure multiple independent loads.

A (linear) calibration matrix maps signals to forces and moments \( f_x, f_y, f_z, \tau_x, \tau_y, \tau_z \), and known sensor geometry can be used to compute contact positions and normals.

\[
V_{\text{out}} = V_{\text{in}} \left[ \frac{R_{g3}}{R_{g3} + R_{g4}} - \frac{R_2}{R_1 + R_2} \right]
\]
Conductive Elastomers

Hillis (1984)

- the separator is used to tune sensitivity, resolution and dynamic range
- prototype with 256 tactile sensors with a spatial resolution of about 1 mm, addressing rows and columns as in a keyboard used 32 wires resulting in a cable diameter of less than 3 mm.
Optical Sensors

“frustration” of total internal reflection \textit{UMass!}

(Begej 1984)

the tactile \textit{image} is conducted away using optical fibers and then subject to image processing
“double refraction” when light passes through anisotropic materials (calcite crystals)

isotropic solids (plastics) under mechanical stress and viewed using two crossed polarizers (transmitted light is rotated by an amount that depends on wavelength) producing chromatic spectra.
Capacitive Sensors

Capacitive Shutter

contact load

capacitor plates

elastic element

fixed dielectric

GLOVE CONDUCTIVE STRIPS

ELASTIC/DIELECTRIC LAYER

FLEXIBLE PRINTED CIRCUIT BOARD

ANALOG MULTIPLEXER "i"

ANALOG MULTIPLEXER "j"

\[ V(t) = -V_0 \cos(\omega_0 t) \]

\[ V_{ij} = \frac{V(t)}{CA} \]
Piezo- and Pyroelectric Effects

$PVF_2$ (polyvinylidene fluoride)

Diagram: Nomenclature:
- epidermal PVF$_2$
- resistive paint
- conductive rubber
- dermal PVF$_2$
- rigid substrate

Signs:
- $V_1 \sim$ deformation and heat flux
- $V_2 \sim$ DC stimulation
- $V_3 \sim$ deformation
Screw Nomenclature

**twist**: generalized velocity
\[ \mathbf{v} \in \mathbb{R}^6 \]
\[ \mathbf{v} = \begin{bmatrix} v_x \\ v_y \\ v_z \\ \omega_x \\ \omega_y \\ \omega_z \end{bmatrix} \]

**wrench**: generalized force
\[ \mathbf{w} \in \mathbb{R}^6 \]
\[ \mathbf{w} = \begin{bmatrix} f_x \\ f_y \\ f_z \\ m_x \\ m_y \\ m_z \end{bmatrix} \]

\(\mathbf{v}\) and \(\mathbf{w}\) do not constitute linear vector spaces!

**power**: \(\mathbf{w}^T \mathbf{v} = [f_x \ f_y \ f_z \ m_x \ m_y \ m_z] \begin{bmatrix} v_x \\ v_y \\ v_z \\ \omega_x \\ \omega_y \\ \omega_z \end{bmatrix}\)
\( v \in V \): object twists consistent with contact constraints; and 
\( \overline{v} \in \overline{V} \): object twists that are restricted by contact constraints.

\[
\text{span}\{V \cup \overline{V}\} = \mathbb{R}^6 \quad \text{and} \quad \{V \cap \overline{V}\} = \{\emptyset\}
\]

for a system of \( n \) contacts to immobilize a body:

\[
\{v_1 \cap v_2 \cap \cdots \cap v_n\} = \{\emptyset\}, \quad \text{and}
\]

\[
\text{span}\{\overline{v}_1 \cup \overline{v}_2 \cup \cdots \cup \overline{v}_n\} = \mathbb{R}^6
\]
Example: Mobility and Constraint in a Planar “Hand”

\[ \begin{align*}
\text{finger #1:} & \quad \begin{bmatrix} v_x \\ v_y \end{bmatrix}_O = \begin{bmatrix} 1 \\ 0 \end{bmatrix}_O \dot{q}_{1a} + \begin{bmatrix} 0 \\ 1 \end{bmatrix}_O \dot{q}_{1p} \\
& = \mathbf{v}_1 \dot{q}_{1a} + \mathbf{v}_1 \dot{q}_{1p} \\
\text{finger #2:} & \quad \begin{bmatrix} v_x \\ v_y \end{bmatrix}_O = \begin{bmatrix} -1 \\ 0 \end{bmatrix}_O \dot{q}_{2a} + \begin{bmatrix} 0 \\ 1 \end{bmatrix}_O \dot{q}_{2p} \\
& = \mathbf{v}_2 \dot{q}_{2a} + \mathbf{v}_2 \dot{q}_{2p} \\
\text{finger #3:} & \quad \begin{bmatrix} v_x \\ v_y \end{bmatrix}_O = \begin{bmatrix} 0 \\ 1 \end{bmatrix}_O \dot{q}_{3a} + \begin{bmatrix} 1 \\ 0 \end{bmatrix}_O \dot{q}_{3p} \\
& = \mathbf{v}_3 \dot{q}_{3a} + \mathbf{v}_3 \dot{q}_{3p}.
\end{align*} \]
Example: Mobility and Constraint in a Planar “Hand”

considering just fingers 1 and 2...

\[ V = \bigcap_{i=1}^{2} v_i = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \bigcap \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} . \]

\[ \implies \] fingers 1 and 2 alone do not fully immobilize the object
Example: Mobility and Constraint in a Planar “Hand”

considering fingers 1, 2, and 3, the intersection of unrestricted object velocities is empty...

\[ V = \bigcap_{i=1}^{3} v_i = \left[ \begin{array}{c} 0 \\ 1 \end{array} \right] \bigcap \left[ \begin{array}{c} 0 \\ 1 \end{array} \right] \bigcap \left[ \begin{array}{c} 1 \\ 0 \end{array} \right] = \emptyset , \]

...these three (fixed) contacts fully immobilize the object,

and the union of velocity constraints derived from active degrees of freedom spans \( \mathbb{R}^2 \):

\[ \overline{V} = \bigcup_{i=1}^{3} \overline{v}_i = \left[ \begin{array}{c} 1 \\ 0 \end{array} \right] \bigcup \left[ \begin{array}{c} -1 \\ 0 \end{array} \right] \bigcup \left[ \begin{array}{c} 0 \\ 1 \end{array} \right] = \mathbb{R}^2 \]

\( \Rightarrow \) the object position fully controllable in the \((x, y)\) plane by the planar hand.
“Form Closure” - Reuleaux (1876)

Definition (Form Closure) - a condition of complete restraint in which any object twist $\in \mathbb{R}^6$ is inconsistent with rigid body assumption for objects and fixed contacts.

*form closure can be defined solely in terms of mobility without specifying contact forces at all*

- Reuleaux
  - planar bodies require at least four frictionless contacts for form closure in $\mathbb{R}^3$, and
  - *exceptional* surfaces exist for which form closure is impossible given any number of frictionless point contacts.

- Somoff (1897) proved that at least 7 frictionless point contacts are necessary for form closure in $\mathbb{R}^6$

- Mishra, Schwartz and Sharir (1987) - established an upper bound of 6 frictionless point contacts on planar objects with piecewise smooth contours, and 12 for the spatial case (except for Reuleaux’s exceptional surfaces).
The Grasp Jacobian

contact coordinate frames
aligned with the
local surface normal

in our planar example, contact frames provide a basis for writing a
linear expression mapping object twists \( \mathbf{v}_O = [v_x \ v_y]^T \) into contact frame twists
\( \mathbf{v}_C = [v_{1x} \ v_{1z} \ v_{2x} \ v_{2z} \ v_{3x} \ v_{3z}]^T \).

\[
\begin{bmatrix}
  v_{1x} \\
v_{1z} \\
v_{2x} \\
v_{2z} \\
v_{3x} \\
v_{3z}
\end{bmatrix}
= \begin{bmatrix}
  0 & 1 \\
  1 & 0 \\
  0 & 1 \\
-1 & 0 \\
  1 & 0 \\
  0 & 1
\end{bmatrix}
\begin{bmatrix}
  v_x \\
v_y
\end{bmatrix}
\]

\[
\mathbf{v}_C = \mathbf{G}^T \mathbf{v}_O
\]

where \( \mathbf{G} = [\mathbf{v}_1 \ \bar{\mathbf{v}}_1 \ \mathbf{v}_2 \ \bar{\mathbf{v}}_2 \ \mathbf{v}_3 \ \bar{\mathbf{v}}_3] \) is the Grasp Jacobian\(^1\)

\(^1\)or Grip Transform [?], Grip Matrix [?], or the Grasp Matrix [?].
Contact Forces

...the power transmitted to the object is equal to the power generated by the contact forces:

\[ \mathbf{w}_O^T \mathbf{v}_O = \mathbf{w}_C^T \mathbf{v}_C \]

since \( \mathbf{v}_C = \mathbf{G}^T \mathbf{v}_O \), we can write

\[ \mathbf{w}_O^T \mathbf{v}_O = \mathbf{w}_C^T [\mathbf{G}^T \mathbf{v}_O], \]

so that,

\[ \mathbf{w}_O^T = \mathbf{w}_C^T \mathbf{G}^T, \text{ or } \]
\[ \mathbf{w}_O = \mathbf{G} \mathbf{w}_C \]

like the manipulator Jacobian, the Grasp Jacobian captures reciprocal velocity and force mappings from contact coordinates to object coordinates.
Force Analysis in the Planar “Hand”

due to the Grasp Jacobian for velocity analysis also defines a transformation from contact loads $\omega_{Ci} = [f_x \ f_z]^T_i$, $i = 1, 3$ to the net wrench on the object $\omega_O = [f_x \ f_y]^T$.

$$
\begin{bmatrix}
    f_x \\
    f_y
\end{bmatrix}_O = 
\begin{bmatrix}
    0 & 1 & 0 & -1 & 1 & 0 \\
    1 & 0 & 1 & 0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
    f_{1x} \\
    f_{1z} \\
    f_{2x} \\
    f_{2z} \\
    f_{3x} \\
    f_{3z}
\end{bmatrix}_C
$$

caveats:

- velocity and force mappings using the Grasp Jacobian do not consider the (in)ability of the hand to generate velocities or forces—e.g. for the planar hand example, $f_{1x} = f_{2x} = f_{3x} = 0$

- to preserve the contact configuration, internal compressive forces are required, e.g. for the planar hand $f_{1z}$ and $f_{2z}$ must be strictly positive (compressive).
## Contact Force Analysis

<table>
<thead>
<tr>
<th>Contact Type</th>
<th>Geometry</th>
<th>Selection Matrix $H^T$ $w_C = H^T \lambda$</th>
<th>Constraints</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frictionless Point Contact</td>
<td></td>
<td>$w_C = \begin{bmatrix} 0 \ 0 \ 1 \ 0 \ 0 \ 0 \end{bmatrix} \begin{bmatrix} \lambda_{fz} \end{bmatrix}$</td>
<td>$\lambda_{fz} \geq 0$</td>
</tr>
<tr>
<td>Point Contact with Friction</td>
<td></td>
<td>$w_C = \begin{bmatrix} 1 &amp; 0 &amp; 0 \ 0 &amp; 1 &amp; 0 \ 0 &amp; 0 &amp; 1 \ 0 &amp; 0 &amp; 0 \ 0 &amp; 0 &amp; 0 \end{bmatrix} \begin{bmatrix} \lambda_{fx} \ \lambda_{fy} \ \lambda_{fz} \end{bmatrix}$</td>
<td>$\lambda_{fz} \geq 0$ $[\lambda_{fx}^2 + \lambda_{fy}^2]^{1/2} \leq \mu \lambda_{fz}$</td>
</tr>
<tr>
<td>Soft Finger</td>
<td></td>
<td>$w_C = \begin{bmatrix} 1 &amp; 0 &amp; 0 &amp; 0 \ 0 &amp; 1 &amp; 0 &amp; 0 \ 0 &amp; 0 &amp; 1 &amp; 0 \ 0 &amp; 0 &amp; 0 &amp; 0 \ 0 &amp; 0 &amp; 0 &amp; 1 \end{bmatrix} \begin{bmatrix} \lambda_{fx} \ \lambda_{fy} \ \lambda_{fz} \ \lambda_{mz} \end{bmatrix}$</td>
<td>$\lambda_{fz} \geq 0$ $[\lambda_{fx}^2 + \lambda_{fy}^2]^{1/2} \leq \mu \lambda_{fz}$ $\lambda_{mz} \leq \gamma \lambda_{fz}$</td>
</tr>
</tbody>
</table>
Rotating Contact Wrenches

given the rotation matrix $\mathbf{O}_R C_i$ that transforms vectors in contact frame $i$ into object frame—the block diagonal

$$
\mathbf{R}_i = \begin{bmatrix}
\mathbf{O}_R C_i & 0 \\
0 & \mathbf{O}_R C_i
\end{bmatrix}
$$

applies this rotation to the force and moment components of the contact wrench independently.
Translating Contact Wrenches

- the force component of the wrench maps to the same forces in the object frame, and
- contact frame moments sum with the “couple” $\mathbf{\rho} \times f_C$, where $\mathbf{\rho} \in \mathbb{R}^3$ is the position vector locating frame $C$ with respect to frame $O$

$$
\mathbf{P}_i = \begin{bmatrix}
1 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 \\
0 & -\rho_z & \rho_y & 1 & 0 & 0 \\
\rho_z & 0 & -\rho_x & 0 & 1 & 0 \\
-\rho_y & \rho_x & 0 & 0 & 0 & 1
\end{bmatrix}
$$

the product of matrix $\mathbf{P}_i$ with a wrench at the contact site transforms that wrench into the equivalent wrench at the object frame.
Constructing the Grasp Jacobian

\[(w_O)_i = G_i w_{Ci} = G_i H_i^T \lambda_{Ci}\]

\[(w_O)_i = G_i^* \lambda_{Ci}, \text{ where } G_i^* = P_i R_i H_i^T.\]

For an \(n\) contact grasp configuration, the grasp Jacobian and effort is written

\[G^* = [G_1^* \cdots G_n^*]\]

and,

\[\lambda = [\lambda_{C1}^T \cdots \lambda_{Cn}^T]^T.\]
Solving for Grasp Forces

Assume that unit contact forces, \( f_i \in \mathbb{R}^3 \), are independent.

**Grasp Jacobian** (by inspection) - \( n \) column vectors describing the body frame wrenches corresponding to each of the \( n \) contact forces.

\[
\mathbf{w}_O = \begin{bmatrix}
\mathbf{w}_1 & \mathbf{w}_2 & \mathbf{w}_3 & \mathbf{w}_4 & \mathbf{w}_5 & \mathbf{w}_6 & \mathbf{w}_7
\end{bmatrix} \begin{bmatrix}
\lambda_1 \\
\lambda_2 \\
\lambda_3 \\
\lambda_4 \\
\lambda_5 \\
\lambda_6 \\
\lambda_7
\end{bmatrix}
\]

\[
\mathbf{w}_O = \mathbf{G}^* \lambda
\]
Prehensile Grasp Stability

the ability of a contact configuration to suppress random disturbances by modifying grip forces

Definition (Force Closure) - A grasp is force closure if a solution for contact frame wrenches $\lambda$ exists that complies with contact type constraints such that

$$G^*\lambda = w_{dist} \quad \text{for arbitrary } w_{dist}$$

$\implies$ the contact configuration is capable of generating a convex envelope of grasp wrench responses (that contains the origin).

*prehensile*
Grasp Stability

...stated in another way...

\[ w_O = G^* \lambda \]

a grasp is force closure (and stabilizable) if and only if \( G^* \) is surjective [Murray, Li, Sastry 1994]

**surjection** ("onto") - every object frame wrench \( w_i \) is accessible by applying transform \( G^* \) to at least one combination of contact frame effort \( \lambda \)

\[ \forall w_i \in W \exists \lambda \in \Lambda\ such\ that\ w_i = G^* \lambda \]
Solving for Grasp Forces

\[ \mathbf{w}_O = \mathbf{G}^* \lambda = \mathbf{G}^* (\lambda_p + \kappa^T \lambda_h) \]

where solutions \( \lambda \) have homogeneous and particular parts,

\[ \lambda = \lambda_p + \kappa^T \lambda_h \]

\( \lambda_h \) is the \textbf{homogeneous part} of the solution and describes combinations of contact forces that impart zero net force to the object.

\[ \mathbf{G}^* \lambda_h = 0 \]

- \( \mathbf{G}^* \) must be full rank to achieve arbitrary reference wrenches
- \( \lambda \) must satisfy inequality constraints for unisense normal forces and contact friction.
Solving for Grasp Forces

\[ \begin{align*}
F_y &= 1 \Rightarrow \lambda_1 + \lambda_4 = 1 \\
M_z &= 0 \Rightarrow -\lambda_1 + \lambda_4 = 0 \\
\Rightarrow \quad \lambda_1 &= \lambda_4 = 0.5 \\
F_z &= 0 \Rightarrow \lambda_2 - \lambda_5 = 0 \\
M_y &= 0 \Rightarrow \lambda_2 + \lambda_5 = 0 \\
\Rightarrow \quad \lambda_2 &= \lambda_5 = 0
\end{align*} \]

frictional constraints
\[
\begin{align*}
\lambda_1 &\leq \mu \lambda_3 \\
0.5 &\leq (0.2)\lambda_3 \\
\lambda_3 &\geq 2.5
\end{align*}
\]

\[
\lambda = \lambda_p + \kappa^T \lambda_h = [0.5 \ 0 \ 0 \ 0.5 \ 0 \ 0 \ 0]_p^T + \kappa [0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0]_h^T
\]

and, \( \kappa \geq 2.5 \) satisfies frictional constraints

suppose: grasp forces must support an object load of \(-1.0\hat{y} \ [N]\) 
\[
M_x = 0 \Rightarrow \lambda_7 = 0 \\
F_y = 0 \Rightarrow \lambda_1 + \lambda_4 = 0 \\
M_z = 0 \Rightarrow -\lambda_1 + \lambda_4 = 0 \\
\Rightarrow \quad \lambda_1 &= \lambda_4 = 0 \\
F_x = 0 \Rightarrow \lambda_3 - \lambda_6 = 0 \\
\Rightarrow \quad \lambda_3 &= \lambda_6
\]

frictional constraints
\[
\begin{align*}
\lambda_1 &\leq \mu \lambda_3 \\
0.5 &\leq (0.2)\lambda_3 \\
\lambda_3 &\geq 2.5
\end{align*}
\]

automated techniques based on mathematical programming are used to solve these systems subject to contact type constraints
1. The grasped object is in quasistatic equilibrium, there are no net forces or moments,

2. all forces are applied within the cone of friction so that there is no slippage, and,

3. an externally applied force can be resisted by finger forces with a finite and controllable deflection.
Grasp Planning

1. Salisbury (1982) - analytical framework for evaluating grasp stability in which the stiffness matrix that characterizes a grasp must be positive definite.

2. Cutkosky (1985) - grasp stability depends on force distributions and local curvature.

3. Montana (1988) - contact grasp stability evaluates the ability of a perturbed grasp geometry to return to an equilibrium configuration—kinematic description of rolling contacts.

4. Nguyen (1989) - all force closure grasps are stabilizable by actively modulating contact forces.


7. Bicchi (1995) - tested force closure and a quality metric for a grasp given friction, contact forces, and constraints on applied forces.
